— Algebra Basics —

# Problem Set #3

# Section A

## Simplify.

1) X + XX·X 2) 3)  $X \cdot X \cdot X \cdot X \cdot X$ X÷X 4) 5) 5X - B + X - B - Y6) -3X - 7 - X + 97) -8 - 2 + 6 - 7 + 48) -5 + -9X - +7 - -2X9)  $(-4)^2$ 10)  $(-4)^3$ 11)  $(-4)^4$ 12)  $30 \div 8 \div 4$ 13)  $10 - 8 \cdot 10^3 \div 4 \cdot 2$ 14) Which fraction isn't equal to the others?

 $(a) \frac{3}{-7} (b) \frac{-3}{7} (c) \frac{-3}{-7} (d) - \frac{3}{7}$ 

**Evaluate each expression** given X = -2; Y = -10; Z = -515)  $X^2 + 2Y - 3Z$ 16)  $Y^2 - 5Z$ 17)  $-Y^2 - 5Z$  $4X - 2YZ + 3Z^{2}$ 18) Solve. 19) a) -X - 5 = -1b) -6X + 3 = -15X20) 36X + 7 = 12X - 521) a)  $\frac{X}{-5} = -30$ b)  $\frac{3}{5}X = -9$ 22) 3(X+2) + 5 = 1 - (X+1)**Section B** Solve. 23) a)  $-4X = -\frac{2}{5}$ b)  $\frac{8}{9} = \frac{12}{X}$ 

24) a) 
$$\frac{8X}{15} = -\frac{12}{5}$$
  
b)  $\frac{-2}{X} = \frac{3}{X-5}$ 

$$25) \qquad 4X - 8 - 10 - 6X = -7 - 3X - 3 + 22$$

26) 
$$4X + 4 + 2(X - 3) = 10 - 6(3X + 4) + 5 - (4X - 7)$$

27) 
$$1\frac{1}{3}X - 3\frac{1}{4} = 5X + 4\frac{1}{2}$$

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- Exponents & Polynomials -

## Problem Set #8 (for groups!)

- 1) Fill in all of the tables on the next page starting with N = 1and going down to N = 10.
- 2) Use the tables to answer the following questions:

a)	What is $3^7$ ?	b)	What is $5^6$ ?
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- c) What is  $2^{10}$ ? d) What is  $10^5$ ?
- 3) On the three's table, every time you move down one step, the answer gets multiplied by 3. Answer the following:
  - a) What happens when you move *down* one step on the five's table?
  - b) What happens when you move *up* one step on the five's table?
  - c) Given that the five's table says that  $5^1 = 5$ , what is the answer when you move one step up to  $5^0$ ? And another step up to  $5^{-1}$ ?
- 4) Fill in each of the tables starting with N = 0 and going up to N = -5. Leave your answers as fractions. (You shouldn't have to do any calculations.)
- 5) Given what you now know, complete each of the following statements:
  - a) Anything to the zero power equals...
  - b) Anything to a negative exponent is the same as...
- 6) Find the values of each of the following:
  - a)  $7^{-2}$  b)  $8^0$  c)  $2^{-10}$
- 7) Rewrite each expression without using a negative exponent:

a) 
$$x^{-5}$$
 b)  $5x^3y^{-4}$  c)  $\frac{3x^{-4}}{5x^3}$ 

--- Factoring ----

# Problem Set #9

Section A

Factor. 1)  $x^2 - x - 20$ 2)  $x^2 + 6x - 36$ 3)  $18x^2 + 31x + 6$ 4)  $14x^2 + 13x - 12$ 5)  $x^2 - 225$ 6)  $x^2 + 225$ 7)  $x^2 + 9x - 20$ 8)  $5x^5 + 20x^3$ Multiply. 9)  $(x^3 - 6)(x^3 + 6)$ 10)  $(x^3 + 6)^2$ 11)  $(x-40)^2$ Solve. 12)  $x^2 - 7x - 30 = 0$ 13)  $x^2 + 25 = 10x$ 14)  $7 + 2x = 8x + x^2$ 15)  $x^2 + 5x = 6$ 16)  $x^2 + 5x + 6 = 0$ 17)  $x^2 + 5x + 6 = 2$ 18)  $x^2 + 5x + 6 = -2x$ 19)  $x^2 + 5x + 6 = 2x^2$ 20)  $x^2 - 54 = 25x$ 21)  $2x^2 - 108 = 50x$ 22) 4(3x-2) = 12x-8 Section B

Multiply. 23)  $4x^{3}(x+3)(x-3)$ 

- (x + 3)(x 3)
- 24)  $(3x 4y^3)^2$
- 25)  $(x^{10}+100)(x^5+10)(x^5-10)$

## Factor.

- 26)  $x^9 x$
- 27)  $12x^3y^5 4x^2y^3$
- 28)  $10x^3 + 10x^2 200x$
- 29)  $8x^2y^5 + 24x^5y^2$
- 30)  $8x^2y^5 + 24x^2y^5$
- 31)  $x^{12} 625$
- 32)  $18x^2 + 12x 6$
- 33)  $18x^2 21xy + 6y^2$
- $34) \quad 18x^6 107x^3 6 \\$

## Solve.

35)  $13 - (x + 3)^2 = 12$ 36)  $5x^2 - 8x + 3 = x^2 + 12x - 21$ 37)  $7x^2 + 3 = x^2 + 19x - 12$ 38)  $x^2 - 56 = (x + 2)(x - 8)$ 39)  $2x^2 - 56 = (x + 2)(x - 8)$ 

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38

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- The Quadratic Formula -

## **Homework**

**Solve** by completing the square.

3)  $x^2 + x - 5 = 0$ 

- 4)  $6x^2 19x + 10 = 0$
- 5)  $3x^2 + 4x + 5 = 0$
- $3x^2 + 4x 5 = 0$

#### **Word Problems**

- 7) The length of a rectangle is 3m more than the width. What are the dimensions if the perimeter is 15m?
- 8) Find the width of a rectangle if twice the width is six feet more than the length, and the area is 80 ft<sup>2</sup>.
- 9) A rectangle has a length of 18 inches and a height equal to the length of the side of a square. Find the side of the square such that the rectangle has an area that is 80 square inches greater than the square.

Solve by the easiest method:

 $x^2 + 9x + 14 = 0$ 

 $x^2 + 5x - 11 = 0$ 

 $3x^2 + 10x + 8 = 0$ 

 $5x^2 + 7x - 10 = 0$ 

10) The length of a rectangle

perimeter is 23 inches, then what are the dimensions?

is 6 inches less than four

times the width. If the

 $x^2 + 6x = 3$ 

Word Problems

# Problem Set #10

5)

6)

7)

8)

9)

## **Group Work**

Solve the equation using each of three methods:

- a) Factoring.
- b) Completing the Square.
- c) The Quadratic Formula.
- 1)  $x^2 + 9x + 20 = 0$

$$2) \quad 6x^2 + 7x - 10 = 0$$

## **Homework**

**Solve** by using each of the three methods:

$$3) \quad x^2 - 6x - 16 = 0$$

**Solve** by quadratic formula:

$$4) \quad 3x^2 - 8x + 4 = 0$$

# Problem Set #11

82

## <u>Homework</u>

- 1) Give the Quadratic Formula.
- 2) The Quadratic Formula is the solution to what equation?
- 3) Give the proof of the quadratic formula.

# **Solve the equation** using each of the three methods (as stated on the previous set):

4) 
$$x^2 - 7x + 12 = 0$$

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